

$$\vec{L} = \vec{R} \times \vec{P}$$

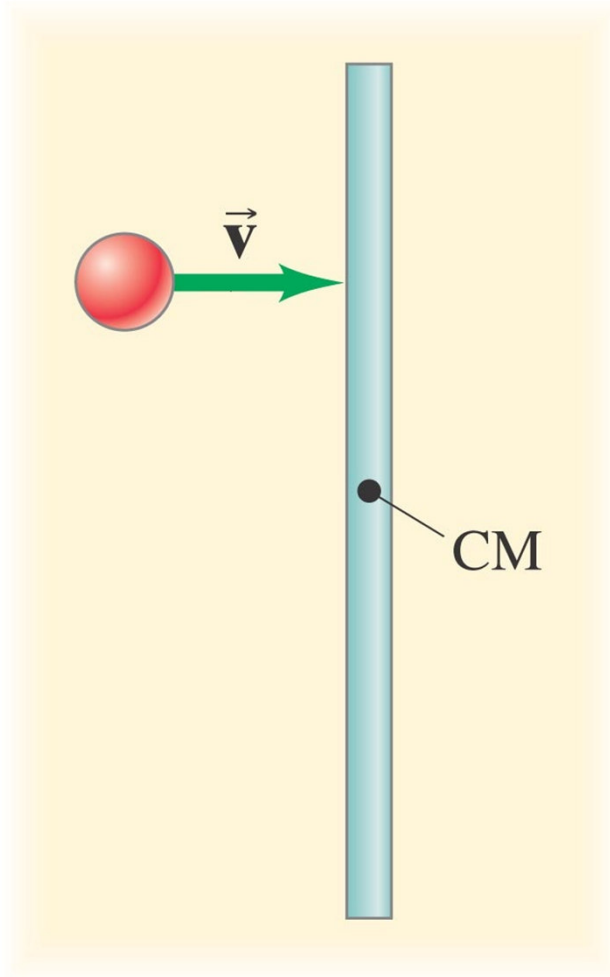
$$\frac{d\vec{L}}{dt} = \frac{d\vec{R}}{dt} \times \vec{P} + \vec{R} \times \frac{d\vec{P}}{dt}$$

$$\frac{d\vec{L}}{dt} = \vec{v} \times m\vec{v} + \vec{R} \times m \frac{d\vec{v}}{dt}$$

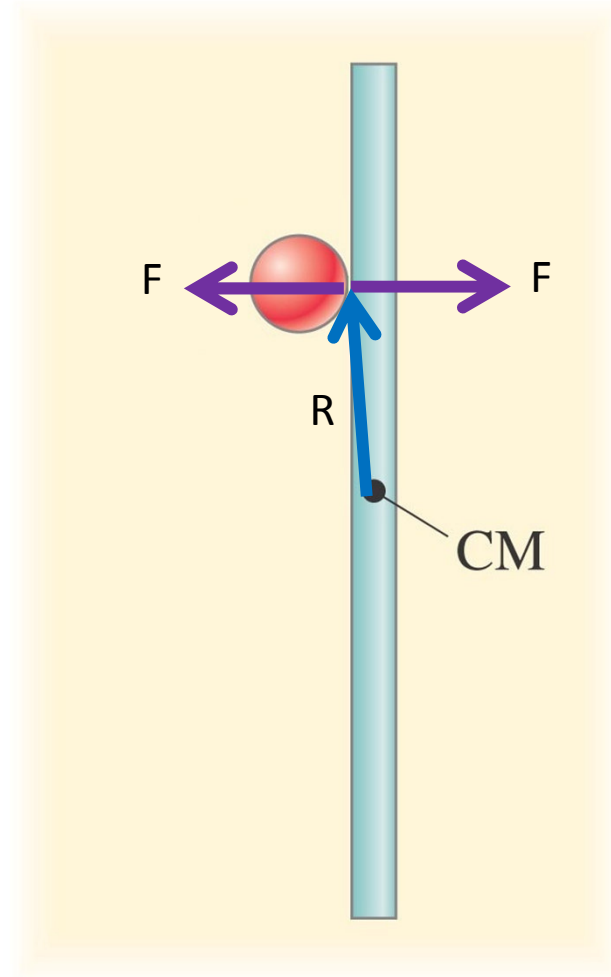
$$\frac{d\vec{L}}{dt} = 0 + \vec{R} \times m\vec{a}$$

$$\frac{d\vec{L}}{dt} = \vec{R} \times \vec{F}$$

$$\frac{d\vec{L}}{dt} = \vec{\tau}$$



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Torques will be equal and opposite!

$$\vec{\tau}_1 = \frac{d\vec{L}_1}{dt}$$

$$\vec{\tau}_2 = \frac{d\vec{L}_2}{dt}$$

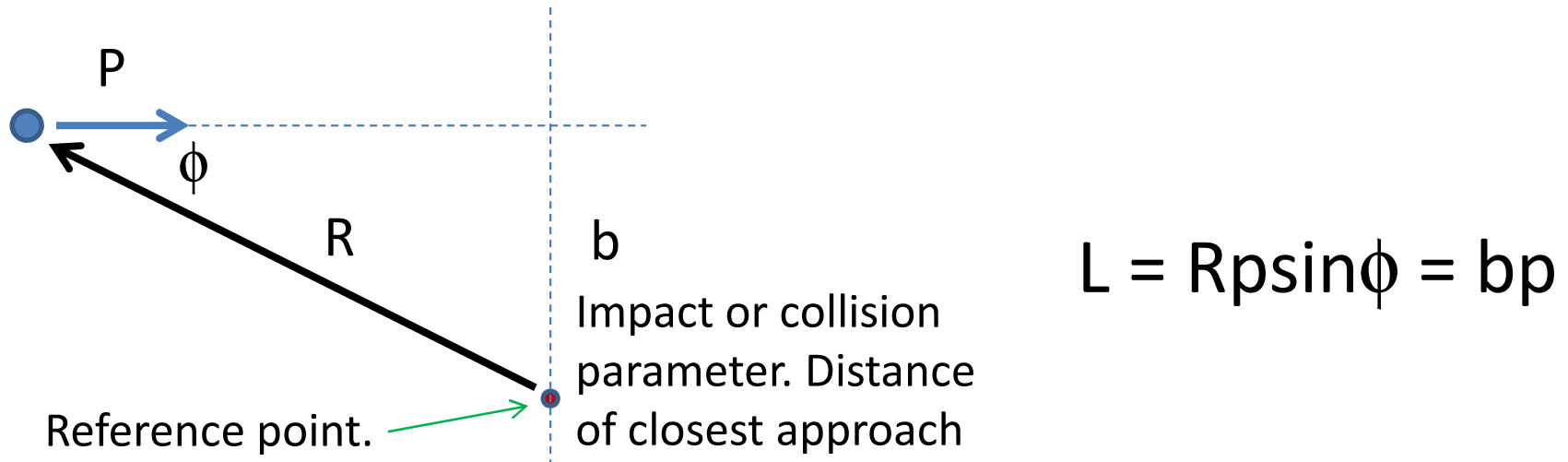
$$0 = \frac{d}{dt} (\vec{L}_1 + \vec{L}_2)$$

$$\vec{L}_f = \vec{L}_i$$

Law of Conservation of Angular Momentum

Special Cases

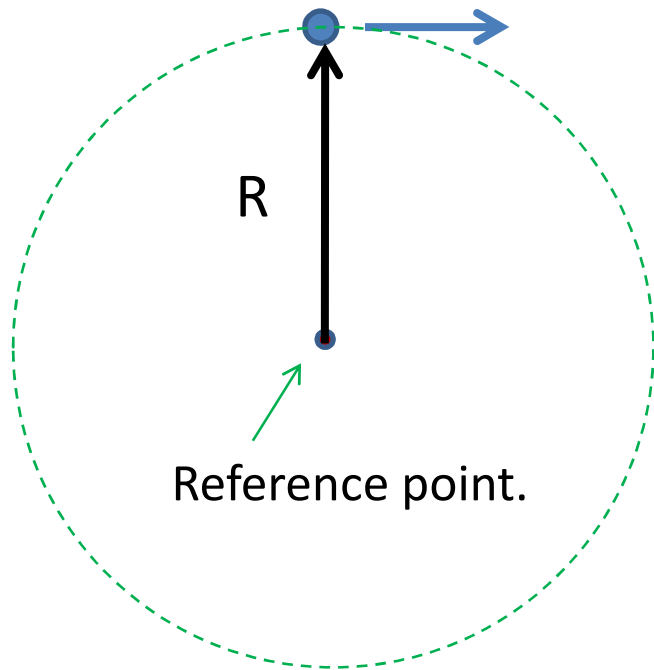
1: Particle Travelling in a Line



If object is not a particle can treat as a particle if size $r \ll b$ and if $l\omega \ll bp$.

Special Cases

2: Particle Travelling in a Circle



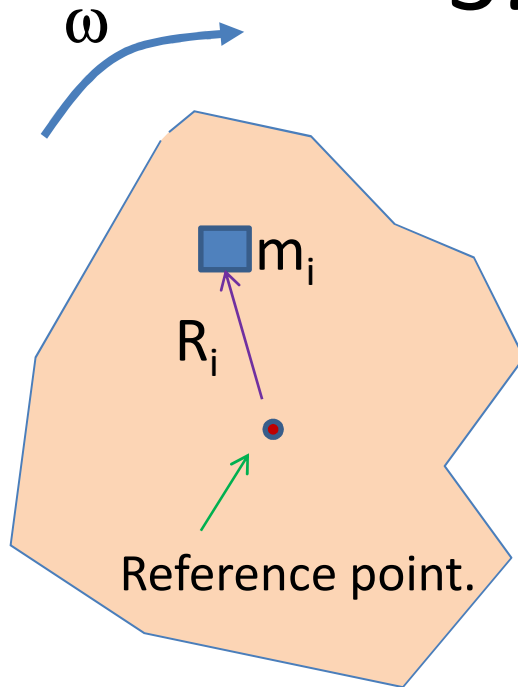
$$L = R p = R m v = R^2 m \omega$$

“Orbital” Angular
Momentum

If object is not a particle can treat as a particle if size $r \ll R$ and if $l\omega \ll b p$.

Special Cases

3: Object Spinning



Consider one particle. It is rotating in a circle.

$$\therefore L_i = m_i R_i^2 \omega$$

For total L add up all the contributions.

$$L = \sum m_i R_i^2 \omega = I \omega$$

“Spin” Angular Momentum

I large,
 ω small

I small,
 ω large

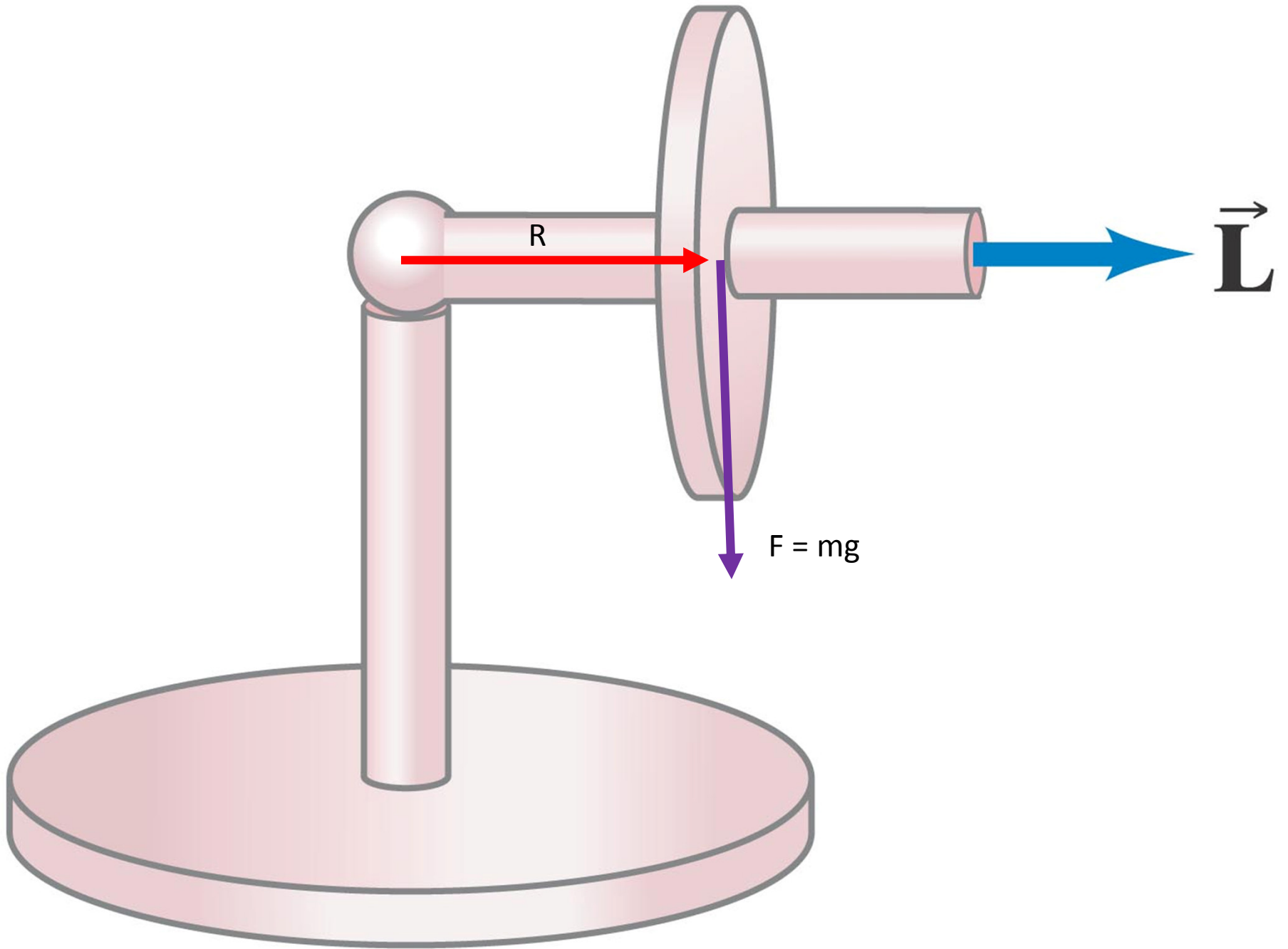


(a)



(b)

Internal forces and torques occur in action-reaction pairs. Angular Momentum is conserved.



Looking from above

