

Terminology:	
Numerator – the number above the fraction line.	$\rightarrow \frac{3}{8}$
Denominator – the number below the fraction line.	
Proper Fraction – a fraction in which the numerator is less than the denominator.	$\frac{3}{4}$
Improper Fraction – a fraction in which the numerator is greater than the denominator.	$\frac{3}{2}$
Mixed Number – a combination of both a whole number	$\longrightarrow 4\frac{5}{8}$

Reciprocal – when the numerator and denominator of a fraction are flipped.

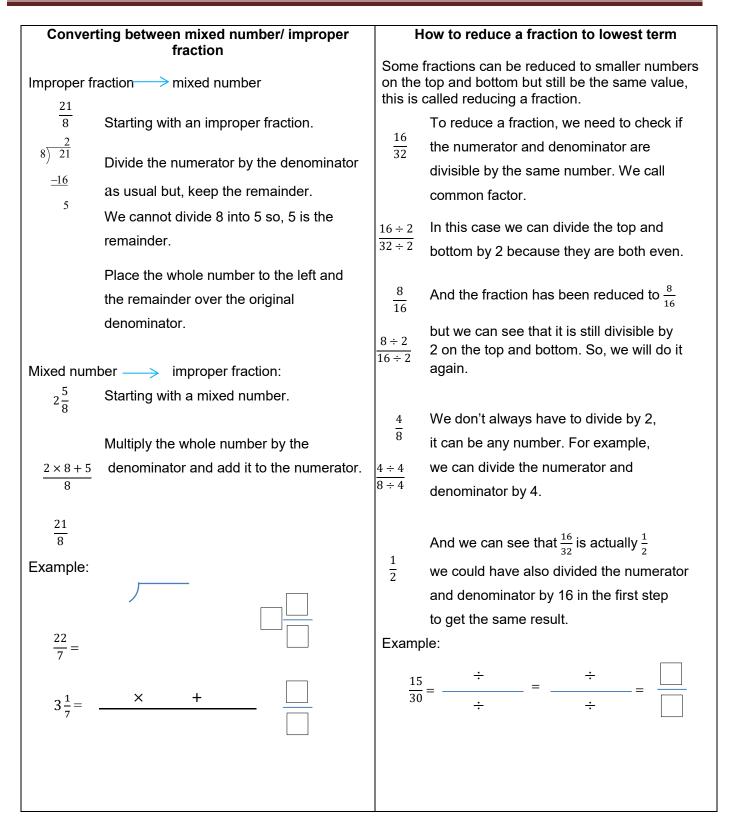
Fraction`	Reciprocal Fraction
$\frac{7}{8}$	$\frac{8}{7}$
<u>Whole</u> <u>Number</u>	<u>Reciprocal of Whole</u> <u>Number</u>
8	$\frac{1}{8}$

Common Denominator – when the denominator of one fraction is equal to the denominator of another fraction.

<u>Common</u>	<u>Non-common</u>
Denominator	Denominator
$\frac{5}{8}, \frac{1}{8}$	$\frac{5}{8}, \frac{1}{3}$









#### **Common Denominators** Finding a common denominator Converting the fractions with the common denominator A common denominator is required when adding or After finding the common denominator, we can subtracting fractions. convert both fractions, so they can be added or subtracted. Be aware not just change the 1 1 To find the Lowest Common bottom of a fraction but also multiple the top 12'16with the same factor, for example: Denominator (LCD) for $\frac{1}{12}$ and $\frac{1}{16}$ . The original fraction is $\frac{1}{12} = 0.0833$ , when you 12 , 16 only change the denominator into 48 without Place both denominators in the changing the numerator, then the faction will be configuration shown. converted to $\frac{1}{12\times 4} = \frac{1}{48} = 0.020833$ . They are obviously not equal. You should multiple the 2 12 16 numerator with the same factor as 4, which Find a number that evenly means $\frac{1 \times 4}{12 \times 4} = \frac{4}{48} = \frac{1}{12} = 0.0833$ divides into both denominators, in this case we will use 2. Place this number to the left. 2 12 16 2 6 8 You may also notice that after 2 12 16 you finish using all the Divide both denominators by the chosen number and place common factors, the the results below. denominator (12) on the left $2 \times 2 \times 3 \times 4 = 48$ side multiplying the bottom **2** 12 16 2 6 8 factor on the right side (4) is LCD=48 Redraw the shape around the equal to 48, the denominator new numbers and pick a new number that evenly divides into on the right side multiplying both, we will use 2 again. the bottom factor on the left $12 \times 4 = 48$ Now no number will evenly go side is also equal to 48, which $16 \times 3 = 48$ into both 3 and 4, so we are done. shows the easy way to get 48 (LCD) from 12 & 16. $2 \times 2 \times 3 \times 4 = 48$ To find the least common Find the LCD of the following groups of fractions: denominator, multiply all the numbers around the outside. $\frac{1}{4}, \frac{3}{16}, \frac{1}{12}, \frac{1}{15}$ $\frac{4}{9}, \frac{5}{6}$ $\frac{1}{8}, \frac{5}{12}$





### Adding Fractions

**Rule for Addition:** When adding any type of fractions, a common denominator is needed. That is, the bottom number of both fractions must be the same.

Fraction + Fract	ion (common denominator)	Fractio	n + Whole Number
$\frac{\frac{5}{16} + \frac{7}{16}}{\frac{5+7}{16}}$ $\frac{\frac{5+7}{16}}{\frac{12}{16}}$	Because these fractions already have a common denominator we do not need to find one. Just add the numbers on top.	$\frac{5}{12} + 5$ $5\frac{5}{12}$	Simply combine the whole number with the fraction as a mixed number
$\frac{12 \div 4}{16 \div 4}$ $\frac{3}{4}$	Reduce the fraction if possible.		
Frac	ction + Fraction	Mixed Nur	nber + Mixed Number
$\frac{1}{12} + \frac{1}{16}$	First find a lowest common denominator.	$1\frac{7}{12} + 2\frac{7}{16}$	Find a lowest common denominator.
$2 \begin{vmatrix} 12 & 16 \\ 2 & 6 & 8 \\ 3 & 4 \end{vmatrix}$ $2 \times 2 \times 3 \times 4 = 48$ $\frac{48}{12} = 4, \qquad \frac{48}{16} = 3$	The lowest common denominator is 48.	$2   12   16  2   6   8  3   4  2 × 2 × 3 × 4 = 48  \frac{48}{12} = 4, \frac{48}{16} = 3$	The lowest common denominator is 48.
$12 \times 4 = 48$		$1\frac{7\times4}{12\times4} + 2\frac{7\times3}{16\times3}$	Convert each fraction.
$16 \times 3 = 48$ $\frac{1 \times 4}{12 \times 4} + \frac{1 \times 3}{16 \times 3}$	Convert each fraction.	$1\frac{28}{48} + 2\frac{21}{48}$ $3\frac{49}{48}$	Now add the whole numbers and add the fractions separately. Convert the improper fraction
$\frac{\frac{4}{48} + \frac{3}{48}}{\frac{7}{48}}$	Now just add the top numbers.	$3 + \frac{49}{48}$ $3 + 1\frac{1}{48}$	portion to a mixed number and add the whole number part to the existing whole number.
		$4\frac{1}{48}$	$\frac{49}{48} = 1\frac{1}{48}$





### **Subtracting Fractions**

Fraction –	Fraction (common denominator)	ons must be the same. Fraction – Fraction	
$\frac{31}{32} - \frac{13}{32}$	Because these fractions already have a common denominator we do not need to find one.	$\frac{5}{6} - \frac{3}{8}$ 2 6 8 3 4	Find the lowest common denominator.
$\frac{31-13}{32}$ $\frac{18}{32}$	Just subtract the top numbers.	$2 \times 3 \times 4 = 24$ $\frac{24}{6} = 4  \frac{24}{8} = 3$	The lowest common denominator is 24.
$\frac{18 \div 2}{32 \div 2}$	Reduce the fraction if possible.	$\frac{5 \times 4}{6 \times 4} - \frac{3 \times 3}{8 \times 3}$ $\frac{20}{24} - \frac{9}{24}$	Convert each fraction. Now subtract the top numbers.
$\frac{9}{16}$		$\frac{11}{24}$	
v	/hole number – Fraction		mber – Mixed Number
$3 - \frac{5}{8}$	Borrow 1 from the whole number and turn it into a	$3\frac{5}{12} - 2\frac{7}{16}$	Find the lowest common denominator.
$2\frac{8}{8} - \frac{5}{8}$	fraction with the same denominator as the subtracting fraction	$4 \ 12 \ 16 \ 3 \ 4$ $4 \times 3 \times 4 = 48$ $\frac{48}{12} = 4 \ \frac{48}{16} = 3$	The lowest common denominator is 48. Convert each fraction.
$2\frac{8-5}{8}$	Keep the whole number and make the fraction portions subtract.	$3\frac{5 \times 4}{12 \times 4} - 2\frac{7 \times 3}{16 \times 3}$ $3\frac{20}{48} - 2\frac{21}{48}$	Now 20-21 would give us a negative number so we mus borrow 1 from the whole number 3.
$2\frac{3}{8}$		$2\frac{1 \times 48 + 20}{48} - 2\frac{21}{48}$	When we borrow one from the whole number, we multiply the base by 1 and add it to the top.
		$2\frac{\frac{68}{48} - 2\frac{21}{48}}{\frac{47}{48}}$	Now subtract the whole numbers and then subtract the tops.





### Multiplying fractions

**Rule for Multiplying:** When doing multiplying, change all items (mixed numbers, numbers) into improper fraction forms first.

Fraction × Fraction		Fraction × Mixed Number		
$\frac{3}{8} \times \frac{17}{32}$	Multiply the numbers beside each other.	$\frac{4}{5} \times 2\frac{1}{3}$	Convert the mixed number to an improper fraction.	
$\frac{3 \times 17}{8 \times 32}$		$\frac{4}{5} \times \frac{7}{3}$	Multiply the numbers beside each other.	
51		$\frac{4 \times 7}{5 \times 3}$		
256		$\frac{28}{15}$	Convert to mixed number.	
		$1\frac{13}{15}$		
Fi	raction $ imes$ Whole number	Mixed Number × Mixed Number		
$\frac{7}{16} \times 4$	Change the whole number to a fraction by placing it over 1.	$1\frac{3}{5} \times 3\frac{2}{8}$	Convert the mixed numbers to improper fractions.	
$\frac{7}{16} \times \frac{4}{1}$	Multiply the numbers beside	$\frac{1}{5} \times \frac{26}{8 \div 8}$	Simplify the numbers if possible.	
$\frac{7 \times 4}{16 \times 1}$	each other.	1	Multiply the numbers beside each other.	
$\frac{28}{16}$		$\frac{26}{5}$		
$\frac{28 \div 4}{16 \div 4}$	Reduce the fraction.	$5\frac{1}{5}$	Convert to a mixed number.	
$\frac{7}{4}$				
$1\frac{3}{4}$	Convert to a mixed number.			





### Dividing fractions

**Rule for Dividing:** When doing dividing, change all items (mixed numbers, numbers) into improper fraction form, then flip the 2<sup>nd</sup> item and change the dividing sign into multiplying.

Fraction + Fraction			action ÷ Mixed Number
$\frac{3}{7} \div \frac{5}{8}$ $\frac{3}{7} \times \frac{8}{5}$ $\frac{3 \times 8}{7 \times 5}$ $24$	Flip the 2nd fraction over (reciprocal) and Change the sign to multiply. Multiply the numbers beside each other.	$\frac{5}{8} \div 1\frac{3}{16}$ $\frac{5}{8} \div \frac{19}{16}$ $\frac{5}{8} \times \frac{16}{19}$ $\frac{5 \times 16}{8 \times 19}$	Convert the mixed number to an improper fraction. Flip the 2nd fraction over (reciprocal) and change the sign to multiply. Multiply the numbers beside each other.
35	tion ÷ Whole Number	$ \frac{80}{152} $ $ \frac{80 \div 8}{152 \div 8} $ $ \frac{10}{19} $ Mixed	Reduce the fraction. d Number ÷ Mixed Number
$\frac{5}{8} \div 3$	Change the whole number to a fraction by placing it over 1.	$2\frac{5}{8} \div 1\frac{1}{6}$ $\frac{21}{8} \div \frac{7}{6}$	Convert the mixed numbers to improper fractions. Flip the 2nd fraction over (reciprocal)
$\frac{5}{8} \div \frac{3}{1}$ $\frac{5}{8} \times \frac{1}{3}$	Flip the 2nd fraction over (reciprocal) and change the sign to	$3\frac{21}{8}\times\frac{7}{8}\times\frac{7}{3}$	and change the sign to multiply. Simplify the numbers if possible.
$\frac{5 \times 1}{8 \times 3}$	multiply. Multiply the numbers beside each other.	$\frac{3 \times 3}{4 \times 1}$ $\frac{9}{4}$	Multiply the numbers beside each other. Check if the answer is reduced to the
5 24		$2\frac{1}{4}$	lowest term. Convert to mixed number if required.

